

NAME ..... SURNAME .....

EXERCISE 1. For which of the following values of  $a$  the equation  $(a^2 + 2a - 3)x = a - 1$  is impossible?

- A  $a = 1$
- B  $a = -3$
- C  $a = 1 \wedge a = -3$
- D  $a = 0$
- E for no value of  $a$

EXERCISE 2. Consider the equation  $\frac{3x + 6}{x^2 - 1} = \frac{2x + 7}{x^2 - 1}$ . Which of the following sentences are true?

- A the existence conditions are C.E.:  $x \neq 1$
- B its only solution is 1
- C it is a fractional equation
- D it is an undetermined equation
- E it is an impossible equation

EXERCISE 3. Consider the two equations  $3x + 1 = 2x + 1$  and  $x(x + 1) = 0$ . Which of the following sentences are true?

- A they have the same degree
- B they are equivalent because they both have the solution 0
- C they are not equivalent
- D the first is in normal form
- E none of the preceding is true

EXERCISE 4. Which of the following numbers is a solution of the equation

$$\frac{4x}{x - 2} = \frac{x + 3}{2 - x} + 1$$

- A  $\frac{3}{2}$
- B 0
- C 2
- D  $-\frac{5}{4}$
- E -3

EXERCISE 5. Which of the following are the existence conditions of the equation

$$\frac{3x - 1}{3x} - \frac{x}{x^2 + 4} = \frac{4}{x^2 - 1}$$

- A  $x \neq 0 \wedge x \neq -2$
- B  $x \neq 0 \wedge x \neq -2 \wedge x \neq 1$
- C  $x \neq 0 \wedge x \neq 1 \wedge x \neq -1$
- D  $x \neq -2 \wedge x \neq -3$
- E none of the preceding

EXERCISE 6. Consider the equation

$$\frac{1}{a}x = 4b$$

Which of the following sentences are true?

- A it is always determined
- B if  $a, b \in \mathbb{Z}$  the solution is an even number
- C if  $a, b \in \mathbb{N}$  and  $a = b$  the solution is a perfect square
- D if  $a = 0$  it is undetermined
- E there is only one value of  $a$  for which the equation has the solution 0

EXERCISE 7. Consider the equation

$$k^2x^2 - 8kx + 15 = 0$$

For what values of  $k$  the equation has 1 as a solution?

- A  $k = 0$
- B  $k = 3 \wedge k = 1$
- C  $k = 5 \wedge k = 0$
- D  $k = 3 \wedge k = 5$
- E for infinite values of  $k$

EXERCISE 8. Consider the equation

$$2ax + b = 8a + b - 6a$$

. Which of the following equations are equivalent to it?

- A  $2ax + b + 5 = 8a + b - 6a + 4$
- B  $2ax + b - b = 8a + b - 6a - b$
- C  $2ax + b + \frac{1}{2} = 8a + b - 6a - \frac{1}{2}$
- D  $2ax + b - 2a = 8a + b - 6a - 2b$
- E none of the preceding

EXERCISE 9. Consider the equation

$$\frac{2}{3} + \frac{1}{3}x = \frac{1}{3}$$

. Which of the following sentences are false?

- A it is a numeric fractional equation
- B it is not an identity
- C it has solution in  $\mathbb{N}$
- D it has solution in  $\mathbb{Z}$
- E it has solution in  $\mathbb{Q}$

EXERCISE 10. Suppose  $a, b$  are two non zero natural numbers. In which of the following cases the equation

$$a^2x + b^2x + abx = a^3 - b^3$$

has the solution in the set of integers  $\mathbb{Z}$ ?

- A always
- B never
- C only if  $a > b$
- D only if  $a \neq b$
- E only if both  $a$  and  $b$  are even numbers

EXERCISE 11. Solve the following fractional equation

$$\frac{2x-1}{x+2} + \frac{1-x}{1+x} = \frac{x-3}{x+2}$$

EXERCISE 12. Discuss and solve the literal equation

$$x(x + a) = x(x - a) + a - 1$$

EXERCISE 13. A purse contains 32 coins, all 50 eurocents and 1 euros. The total value of the money is 25.50 euros. How many coins are there of each kind?